

Dynamic Banking and the Value of Deposits

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Abstract

We propose a dynamic theory of banking where deposits play the role of productive capital as in the classical Q-theory of investment for non-financial firms. A key conceptual innovation of our theory is that the stock of deposits cannot be perfectly controlled by the bank. Demand deposit accounts commit the bank to allow holders to withdraw or deposit funds at will without prior notice. The resultant uncertainty in deposit flows exposes banks to the risk of violating regulatory restriction on leverage. In our theory, the equity capital-to-deposit ratio is the key state variable affecting bank valuation and decision making. Deposits generally create value for banks except when the bank is close to hitting the leverage restriction, because sudden deposit inflows can force banks into costly equity issuance. We show that banks are endogenously risk averse with respect to both the deposit flow risk and standard loan return risk. Our model predictions on dynamic bank valuation and asset-liability management are broadly consistent with the evidence. Moreover, our model lends itself to a quantitative evaluation of the costs and benefits of leverage regulations.

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1 Introduction

During the global financial crisis, and more recently during the unfolding COVID-19 pandemic, banks have been subject to large deposit inflows and outflows. The largest and safest banks have undergone large increases in their balance sheets as a result of massive inflows of funds into deposit accounts, while weaker banks have suffered from deposit outflows. Most dramatically, just in April 2020, deposits of US banks increased by \$865 billion. From Q4 2019 to Q1 2020, JPMorgan Chase experienced an increase of 18% percent of its deposit base, and the deposit liabilities of Citigroup and Bank of America increased by 11% and 10%, respectively.¹

Large deposit flows are both a risk and an opportunity for banks. As the literature has emphasized, the bank business model rests on deposit taking. Demand deposit account is a source of cheap funding that banks rely on to finance their lending and trading activities. Depositors accept relatively low rates for the convenience of using deposits as means of payment. But the consequence of depositors' freedom to move funds in and out of their deposit accounts is that banks cannot perfectly control the size of their deposit base and balance sheet. To the extent that the banking literature is modeling such risk, it has done so only in terms of the bank run risk. Such models assume that, in the no-run equilibrium, banks face no risk with respect to the size of deposit base so that deposits can be treated as fixed-maturity debts.

We depart from this narrow framing and treat banks' deposit base more generally as randomly evolving and subject to shocks of both inflows and outflows. In our dynamic model of the banking firm, deposits have random maturity, and the deposit base is a sticky and stochastic variable that is only partially controllable. The size of deposit liabilities as a randomly evolving variable is one of the key features that distinguishes a bank from a non-financial firm. The other important distinguishing feature is that banks are subject to capital regulations. To be able to continue operating, a bank must make sure that its equity capital remains above a minimum required amount. Importantly, due to the deposit risk, a bank does not have full control over the ratio of equity capital to deposits, which is the key endogenous state variable in our model.

¹See "U.S. Banks are 'Swimming in Money' as deposits increase by 2 trillion dollars amid the coronavirus" by Hugh Son, CNBC June 21, 2020. <https://www.cnbc.com/2020/06/21/banks-have-grown-by-2-trillion-in-deposits-since-coronavirus-first-hit.html>

We add two important frictions to this model. First, we assume in line with the evidence that it is costly for banks to issue new equity. Second, we assume that there is a lower bound for the remuneration of deposits. A natural lower bound is zero, but we can also allow for a negative lower bound that accounts for various fees. In practice, banks are loath to impose negative rates on deposits even if this could help stem an inflow of new deposits and the associated involuntary expansion of leverage. Empirically, this deposit rate lower bound has become increasingly binding in the current low-rate environment. The combined effect of these two frictions is that a bank is endogenously risk-averse. When the bank's equity capital-to-deposit ratio is low, a sudden increase in deposits could cause a violation of the leverage restriction, which forces the bank to pay the issuance (dilution) costs and raise equity. In this region, the marginal value of additional deposits is low, even sharply negative. In contrast, when the bank is well capitalized (i.e., when it has a high equity capital-to-deposit ratio), the marginal value of deposits is high, as deposits represent cheap financing for lending with a low risk of violating the regulatory constraint.

For tractability we do not add any other frictions that may be relevant in practice. One important friction that is absent from our model is fire-sale pricing, which happens when a bank seeks to quickly shrink its asset base, or other forms of adjustment costs in changing the bank's assets. For simplicity, the bank can costlessly change the size of its asset portfolio in our model. This is a reasonable assumption for financial securities, which can be quickly adjusted at low costs. Admittedly, this is a stronger assumption as far as the bank's loan book is concerned. Adding an adjustment cost to the bank's loan book, however, is a major complication as this would introduce a second state variable, rendering the mechanism much less transparent.

We characterize the bank's dynamic asset-liability management decisions including optimal deposit remuneration, short-term borrowing, lending, equity issuance, and dividend payout in the presence of regulatory constraints. We solve for the franchise value of the bank and how it varies with the equity capital-to-deposit ratio. We also solve for the marginal value of deposits and show that it decreases as the bank approaches the regulatory constraints.

Because it is costly to issue equity, the marginal value of equity capital is larger than one, and depends on the value of equity capital-to-deposit ratio, denoted by k , which is bounded by

two endogenous reflecting boundaries. The marginal value of equity capital varies over a wide range: it is equal to one at the dividend payout boundary, when k is high and the bank is indifferent between retaining an extra unit of capital or paying it out (that is how the endogenous upper bound is defined), and when k is low, it can rise to above four at the equity issuance boundary (the lower bound of k), even under conservative values for the issuance costs from the empirical literature. When the bank is close to hitting its regulatory leverage restriction, any additional unit of equity capital is very valuable as it reduces the likelihood of costly equity issuance.

The marginal value of equity capital does not decline with k linearly. The bank's franchise value is strictly concave in k , so that the bank is endogenously risk-averse even though shareholders are assumed to be risk neutral. We show that it is optimal for the bank to substantially reduce lending as k declines and the bank approaches the regulatory constraint. This is consistent with empirical findings linking changes in bank equity capital to changes in bank lending. When k increases and does approach the payout boundary, it is more likely to stay around than not. Indeed, at the peak of the stationary density of k the marginal value of equity is only slightly above one, so that, for the majority of time, the bank does not seem to be financially constrained. This nonlinearity captures a sharp contrast between the normal times and the crisis times when k is low, close to the equity issuance boundary, and the marginal value of equity capital shoots up dramatically.

In our model, deposits are valuable because, enjoying the convenience of payment services, depositors are willing to accept a deposit rate that is below the prevailing risk-free rate. When the bank has sufficient equity capital, deposits create value by allowing the bank to finance risky lending with cheap sources of funds. The deposit stock in effect serves as a form of productive capital for the bank. However, when the bank's equity capital is depleted, the marginal value of deposits can be negative. The reason is that, near the costly issuance boundary, uncontrollable deposit inflows destroy value for the bank's shareholders by increasing the bank's leverage and amplifying the likelihood of costly equity issuance in compliance of leverage restriction. The bank then wants to deleverage and turn away deposits. However, the bank can only go as far as setting the deposit rate at the lower bound; it cannot turn down deposits by further lowering the rate.

Losing control of its deposit base is a problem when the bank faces equity issuance costs,

for then, in effect, it also loses control of its leverage. Indeed, we show that without the equity issuance costs the bank can costlessly offset any increase in deposits with a commensurate amount of newly raised equity capital, thereby maintaining its leverage at the desired level. The bank's franchise value is then linear in k , so that the bank is no longer endogenously risk averse.

In our model, a sharp distinction is drawn between deposits and short-term debt. With short-term debt, the bank can always choose to stop borrowing at maturity, and therefore, does not face the problem of unwanted debt. Deposits do not have a well-defined maturity. Deposits leave the bank only when depositors chose to withdraw funds (for example, to pay other banks' depositors or for cash withdrawal). Hence, deposits add value only if the bank has sufficient equity capital and thus is not at the risk of costly equity issuance in compliance of regulatory requirements.

Given that the bank is endogenously risk averse, it wants to hold safe assets for precautionary reasons when the equity capital-to-deposit ratio, k , is low, but when k is high, the bank switches its position in risk-free assets, issuing short-term debt to obtain an even higher leverage than the leverage already obtained through deposit-taking. Such procyclicality is again due to the risk with respect to uncontrollable deposit flows. Specially, when k is small and the bank is close to violating the regulatory constraint, it deleverages by simultaneously reducing short-term debt and lowering the deposit rate to turn away deposits. When the bank has eliminated short-term debt and is close to the deposit rate lower bound, it almost loses control of its liability structure. As a result, to avoid violating costly equity issuance, the bank has to work on the asset-side of its balance sheet, tuning down its exposure to loan risk by holding risk-free assets. When k is large and the bank is sufficiently away from the equity issuance boundary, its risk-taking incentive is strong and results in a switch from the bank holding risk-free assets to raising short-term debt for risky lending.

Literature. In the banking literature, the focus is on bank runs when it comes to banks' commitment to allow depositors to withdraw funds without prior notice (see, e.g., Diamond and Dybvig, 1983; Allen and Gale, 2004b; Goldstein and Pauzner, 2005). However, the deposit flow risk is more ubiquitous than the dramatic bank runs and influences banks' daily operation. Moreover, it is not just deposit outflow that poses a challenge to banks. Deposit inflow can also be a risk, especially in the presence of regulatory constraints and equity issuance costs.

Depositors are willing to accept relatively low rates because of the convenience of using deposits as means of payment. What enables deposits as money is precisely banks' commitment to allow depositors to move funds in and out of their accounts. Banks are thus exposed to large payment inflows and outflows at high frequencies (Denbee, Julliard, Li, and Yuan, 2018). The maturity of deposit liabilities is not chosen by the bank. It often depends on depositors' payment needs that are uncertain. With a diversified depositor base, a bank essentially views deposits as debts that retire at a stochastic rate. Bianchi and Bigio (2014) and De Nicolò, Gamba, and Lucchetta (2014) also recognize such payment shocks. However, in their models, deposits are one-period contracts (with intra-period shocks), so banks can freely adjust the deposit base every period. In contrast, deposit contract in reality (and in our model) is infinite-horizon – depositors can freely hold deposits as long as they want. To adjust deposit base, banks can change deposit remuneration but completely loses control of deposit base when its deposit rate hits the lower bound.² The key to our main results is precisely banks' lack of control of the deposit base, which exposes banks to the risk of paying equity issuance costs to stay in compliance with the regulatory requirements.

Deposits are inside money of the private sector – stores of value and means of payment issued by banks to depositors. This feature has been well recognized in the recent macro-finance literature. However, deposits are modelled as short-term debts (e.g., Piazzesi and Schneider, 2016; Drechsler, Savov, and Schnabl, 2018) with interest rates below the prevailing rate by a money premium (Stein, 2012; DeAngelo and Stulz, 2015; Krishnamurthy and Vissing-Jørgensen, 2015; Greenwood, Hanson, and Stein, 2015; Li, 2019; Begenau, 2019). Brunnermeier and Sannikov (2016) is a notable exception. They model deposits as infinite-maturity nominal liabilities. Dynamic banking models typically differentiate short-term debts and deposits in their interest rate and operation costs (Hugonnier and Morellec, 2017; Van den Heuvel, 2018; Begenau, 2019). However, in all the models, banks do not face uncertainty in the size of deposit liabilities.

²Depositors' response to changes in remuneration is sluggish, which is a feature emphasized by studies on banks' deposit market power (Drechsler, Savov, and Schnabl, 2017).

2 Model

We model a single bank's decisions under the risk-neutral measure, effectively assuming no arbitrage and taking as exogenous the pricing kernel (stochastic discount factor) that depends on the aggregate dynamics of the broader economy. Let r denote the risk-free rate, which is also the expected return of all financial assets under the risk-neutral measure.

Risky assets. We use A_t to denote the value of the bank's holdings of loans and other investments at time t .³ It has the following law of motion:

$$dA_t = A_t(r + \alpha_A) dt + A_t \alpha_A d\mathcal{W}_t^A; \quad (1)$$

The parameter α_A reflects the return from the bank's expertise. Because we set up our model under the risk-neutral measure, α_A is the risk-adjusted value-added.⁴ The second term in (1) describes the Brownian shock, where α_A is the diffusion-volatility parameter and \mathcal{W}^A is a standard Brownian motion. Examples of these shocks include unexpected charge-offs of delinquent loans. At any time t , the bank may adjust its risky assets and the liability structure (i.e., deposits, bonds, and equity).

Deposits. Deposits are at the core of our model. Let X_t denote the value of deposits at time t on the liability side of the bank's balance sheet. It has the following law of motion:

$$dX_t = -X_t(\lambda_X dt - \lambda_X d\mathcal{W}_t^X) + X_t n(i_t) dt; \quad (2)$$

where \mathcal{W}_t^X is a standard Brownian motion. Given a diversified depositor base, a $(\lambda_X dt - \lambda_X d\mathcal{W}_t^X)$ fraction are withdrawn in dt because depositors may need cash or pay agents who hold accounts at other banks. If $(\lambda_X dt - \lambda_X d\mathcal{W}_t^X) > 0$, the bank's own depositors receive payments into their

³The bank's assets include not only loans but also other assets that generate revenues of trading and services such as cash management, trade credit, derivatives, structured products, and underwriting of securities (Bolton, 2017).

⁴The bank may have expertise in loan screening (Ramakrishnan and Thakor, 1984), monitoring (Diamond, 1984), relationship lending (Boot and Thakor, 2000), restructuring (Bolton and Freixas, 2000), and serving local markets (Gertler and Kiyotaki, 2010). More generally, in the macro-finance literature, banks are often modelled as agents with expertise in asset management (He and Krishnamurthy, 2012, 2013; Brunnermeier and Sannikov, 2014, 2016).

accounts. Deposits thus have an average *effective duration* of $1 - \alpha$, and α captures payment flow uncertainty.⁵ The stochastic withdrawal is in line with the three-dates models (see, e.g., Diamond and Dybvig, 1983; Allen and Gale, 2004b), where agents' stochastic preferences over early and late consumption translate into uncertainty in the deposit outflow. The deposit flow shock, $d\mathcal{W}_t^X$, is likely to be positively correlated with the loan repayment shock, $d\mathcal{W}_t^A$, as a healthy asset portfolio can attract depositors. Let σdt denote the instantaneous covariance between $d\mathcal{W}_t^X$ and $d\mathcal{W}_t^A$.

In the presence of diffusive shocks (instead of jump shocks), the bank can avoid default by adjusting the balance sheet locally and thus preserve a positive continuation value for equityholders. Therefore, deposits are risk-free for depositors. The deposit rate is i_t , chosen by the bank. The spread, $r - i_t$, can be positive if agents value the convenience of deposits as means of payment (e.g., DeAngelo and Stulz, 2015; Nagel, 2016; Piazzesi and Schneider, 2016; Li, 2019, 2018) or value the secondary-market liquidity due to deposits' information-insensitivity (e.g., Gorton and Pennacchi, 1990; Holmström, 2012; Dang, Gorton, Holmström, and Ordóñez, 2014).

The bank can adjust the growth rate of deposit stock by setting i_t via $n(i_t) dt$, where the deposit demand elasticity depends on the bank's deposit market power (Drechsler, Savov, and Schnabl, 2017). When the deposit rate is very low, we can have $n(i_t) < 0$. Moreover, following Hugonnier and Morellec (2017), we assume that to maintain the existing deposits and attract new deposits, the bank pays a flow cost $C(n(i_t); X_t) dt$, for example, from operating branches.

Deposits are essentially long-term debts with stochastic maturity and controllable increments. Not all depositors withdraw at the same time, and withdrawal depends on depositors' payment needs. Therefore, a diversified depositor base implies an effective duration of deposits that depends on the average rate of withdrawal. Our treatment of deposits stands in contrast with the macro-finance literature and dynamic banking literature that generally treats deposits simply as short-term debts (motivated by depositors' right to withdraw at any time). We emphasize that the right to withdrawal does not necessarily translate into a low duration of deposits but rather imposes a lower bound on the feasible deposit rate – the bank cannot set a negative deposit rate because depositors will withdraw en masse and earn the zero return on dollar bills. We assume that in such

⁵The value of α largely depends on where the bank sits in the payment network, and the payment flow uncertainty α can be significant in data (see, e.g., Denbee, Julliard, Li, and Yuan, 2018).

a bank run, the shareholders' equity is wiped out, so the bank always avoids such scenario. In reality, depositors may tolerate an effective negative deposit rate due to various fees, but as long as there exists a lower bound, our results hold.

Bonds. The bank issues short-term bonds (e.g., financial commercial papers), and it is costless to do so. Let B_t denote the value of bonds issued at t that will mature at $t + dt$. Without default risk, the contractual rate of return for short-term debt initiated at t is the risk-free rate r . The bank's bond interest payment over time interval dt is $B_t r dt$. The bank may choose not to issue bonds but instead invest in risk-free bonds issued by other entities in the economy (e.g., the government). In this case, we have $B_t < 0$. Whether the bank issues or holds risk-free bonds will depend on its risk-taking capacity, which in turns depends on the existing deposit liabilities and equity capital.

Equity, Dividend, and Costly Issuance. Let K_t denote the bank's equity (or "capital"), so the following identities summarizes all the balance-sheet items:

$$K_t = A_t - (B_t + X_t) : \quad (3)$$

The bank can pay out dividends that reduce K_t . We use U_t to denote the (undiscounted) cumulative dividends, so the amount of (non-negative) incremental payout is dU_t . The bank may find it optimal to issue external equity. In reality, banks face significant external financing costs due to asymmetric information and incentive issues.⁶ A large empirical literature has sought to measure these costs, in particular, the costs arising from the negative stock price reaction in response to the announcement of a new equity issue.⁷ Let F_t denote the bank's (undiscounted) cumulative net

⁶Explicitly modeling informational asymmetry would result in a substantially more involved analysis. Lucas and McDonald (1990) provides a tractable analysis by making the simplifying assumption that the informational asymmetry is short lived, i.e. it lasts one period.

⁷Lee, Lochhead, Ritter, and Zhao (1996) document that for initial public offerings (IPOs) of equity, the direct costs (underwriting, management, legal, auditing and registration fees) average 11.0% of the proceeds, and for seasoned equity offerings (SEOs), the direct costs average 7.1%. IPOs also incur a substantial indirect cost due to short-run underpricing. An early study by Asquith and Mullins (1986) found that the average stock price reaction to the announcement of a common stock issue was -3% and the loss in equity value as a percentage of the size of the new equity issue was as high as -31% (see Eckbo, Masulis, and Norli, 2007, for a survey).

external equity financing up to time t and H_t to denote the corresponding (undiscounted) cumulative costs of external equity financing up to time t . Following Bolton, Chen, and Wang (2011), we assume that the bank incurs both fixed and proportional costs of issuing equity. To preserve the model's homogeneity property for tractability purposes, we further assume that the fixed cost is proportional to X_t , so that $\phi_0 X_t$ denotes the fixed equity-issuance cost, and $\phi_1 M_t$ refers to the proportional equity-issuance cost, where M_t is the amount raised.

The bank's equityholders are protected by limited liability. Let τ denote the stochastic stopping time when the bank defaults. Therefore, the bank maximizes the equityholders' value,

$$V_0 = \mathbb{E} \left[\int_{t=0}^{\tau} e^{-rt} (dU_t - dF_t - dH_t) \right].^8 \quad (4)$$

Because the bank only faces (locally continuous) diffusive shocks, it can avoid default as long as the continuation value is positive. In our numeric solution, this is indeed the case, so $\tau = +\infty$. We assume that the discount rate r , i.e., the equityholders' required return, is greater than ρ . This impatience can be microfounded by a Poisson death rate that is equal to $\rho - r$. In our numeric solution, we calibrate the spread to banks' exit rate. Note that K_t is the book value of equity and V_t , the equityholders' value at t , is the market value of equity. In perfect capital markets à la Modigliani and Miller (1958), $V_t = K_t$. However, as we will show shortly, $V_t > K_t$ due to the equity issuance cost. The wedge between V_t and K_t measures the value of internal capital.

Capital requirement. The bank must meet a capital requirement. For example, the Basel III accords stipulate that banks must back a specific percentage of risk-weighted assets with equity.⁹ As in Begenau (2019), Davydiuk (2017), Nguyen (2015), and Van den Heuvel (2018), we introduce

$$\frac{A_t}{K_t} \leq \kappa. \quad (5)$$

⁸We assume that the bank manager's incentive is aligned with equityholders. Becht, Bolton, and Röell (2011) discuss the issues of corporate governance in the banking sector.

⁹See Thakor (2014) for a review of the debate on bank capital and its regulations.

In accordance with Basel III capital standards, banks must maintain the Tier 1 capital ratio (Tier 1 capital divided by total risk-weighted assets) of 6% (increased to 7% from 2019 onward) (see, e.g., Begenau, 2019; Davydiuk, 2017). We set κ equal to $1/0.07 = 14.3$.¹⁰

Leverage ratio requirement. Since January 1, 2018, banks in the U.S. face a supplementary leverage ratio restriction (SLR). It supplements the capital requirement that can be vulnerable to manipulation (Plosser and Santos, 2014). Banks are required to maintain a ratio of tier 1 capital to total consolidated assets at a minimum level of 3%. The U.S. bank holding companies that have been identified as global systemically important banks (“U.S. G-SIBs”) must maintain an SLR of greater than 5%, and if they fail to do so, they will be subject to increasingly stringent restrictions on its ability to make capital distributions and discretionary bonus payments.¹¹

The ratio of its total assets (or liabilities) to equity capital cannot exceed L . When the bank has short-term debts, i.e., $B > 0$, the leverage ratio requirement is given by

$$\frac{A}{K} = \frac{K + X + B}{K} \leq L; \quad (6)$$

and when $B < 0$, the leverage ratio requirement is given by

$$\frac{A - B}{K} = \frac{K + X}{K} \leq L; \quad (7)$$

SLR capital requirement of 5% translates into $L = 20$. We set $L = \kappa = 14.3$ (denoted by) so that, when $B > 0$, capital requirement and SRL restriction coincide. Moreover, banks may

¹⁰Begenau (2019) and Davydiuk (2017) set κ to be the sample average of the ratio of Tier 1 equity to risky assets in their models for the reason that banks typically maintain a buffer over the regulatory thresholds in order to prevent regulatory corrective action. In our model, the buffer arises endogenously, driven by banks’ precaution to avoid paying the equity issuance costs, so we set κ to the regulatory threshold. In other studies on banking regulations, De Nicolò, Gamba, and Lucchetta (2014) calibrates the capital requirements to 4% and 12%, Hugonnier and Morellec (2017) calibrates the thresholds to 4% , 7%, 9%, and 20% to investigate the effects of the proposal by Admati and Hellwig (2013), and Phelan (2016) calibrates the threshold to 7.7% and 10.6% in a macroeconomic model.

¹¹During the Covid-19 crisis, the U.S. regulators excluded Treasury securities and reserve held at the Federal Reserve System from the denominator of SLR, as banks faced an influx of deposits on the liability side of their balance sheets and, on the asset side, acquired significant amounts of U.S. Treasury securities and news loans (especially due to customers drawing on credit lines).

self-impose a tighter SLR requirement to avoid reputation costs from regulatory intervention.

3 Dynamic Banking without Equity Issuance Costs

A key friction in our model is the equity issuance cost. Next, we show that without such costs, the value function is linear in the deposit stock, X , and capital, K . As a result, the bank does not exhibit endogenous risk aversion and the marginal value of deposits is constant.

Without the issuance costs, the marginal value of capital is equal to one, i.e., $V_K(X; K) = 1$, because if $V_K(X; K) > 1$, the bank will raise equity, and, as previously discussed, the bank pays out dividend if $V_K(X; K) \leq 1$. In Appendix A, we show that there exists a constant Q such that

$$V(X; K) = QX + K : \tag{8}$$

A key result is that Q does not depend on any of the risk parameters, i.e., σ_A and σ_X . Without the equity issuance costs, the bank is not concerned about risks because when it needs capital following adverse shocks, it can always raise capital. Intuitively, as long as $\sigma_A > 0$, i.e., lending generates excess return, the bank will borrow short-term debt, increasing leverage beyond what is already obtained through deposit-taking. As previously discussed, when $B > 0$, the capital requirement and the SLR restriction coincide. The bank's optimal lending is proportional to equity capital and the capital requirement (or, equivalently the SLR restriction) always binds, i.e., $A=K = \kappa$. Moreover, the bank sets a constant deposit rate. I will compare these properties with those of the solution under the equity issuance costs.

4 Dynamic Banking under Equity issuance Costs

4.1 Bank Optimization

We derive the optimality conditions for the bank's control variables and the Hamilton-Jacobi-Bellman (HJB) equation for the bank's value function. In the next subsections, we parameterize

the deposit maintenance cost and provide intuitive characterizations of the bank's optimal policies.

State and control variables. The bank solves a dynamic optimization problem with two state variables, the deposit stock X_t and the equity capital K_t . We denote the shareholders' value at time t as V_t . This present value results from the bank's optimal control of the stochastic processes of loan portfolio size A_t , short-term borrowing B_t , the deposit rate i_t , the payout of dividends dU_t , and the value of newly issued equity shares dF_t :

$$V_t = V(X_t; K_t) = \max_{fA; B; i; U; Fg} \mathbb{E} \left[\int_{t=0}^{\infty} e^{-\rho t} (dU_t - dF_t - dH_t) \right] : \quad (9)$$

The value function is a function of the state variables, i.e., $V_t = V(X_t; K_t)$. Every instant, given the state variables, X_t and K_t , the bank optimizes the control variables before the realization of diffusion shocks, taking into consideration the impact on the evolution of state variables (and through such impact, the continuation value). To solve the bank's optimal choices and value function, we need the laws of motion of state variables that show how the choice variables affect their evolution. The law of motion for X_t is given by (2). For the equity capital K_t , we have

$$dK_t = A_t [(r + \lambda_A) dt + \sigma_A dW_t^A] - B_t r dt - X_t i_t dt - C(n(i_t); X_t) dt - dU_t + dF_t : \quad (10)$$

The first three terms on the right side record the return on loans, bond interest expenses, and deposit interest expenses. The fourth term is the operation cost associated with adjusting and maintaining the deposit stock. The last two terms are the dividend payout and capital raised via equity issuance.

Given X_t and K_t , the bank's choices of A_t and B_t resemble a portfolio problem (Merton, 1969).¹² Let α_t^A denote the portfolio weight on loans, i.e., $\alpha_t^A (X_t + K_t) = A_t$, so the weight on bonds is $(\alpha_t^A - 1)$ because $B_t = A_t - (X_t + K_t)$. Note that if $A_t > X_t + K_t$, the bank issues bonds, $B_t > 0$, paying the interest rate r ; if $A_t < X_t + K_t$, the bank lends in the short-term debt

¹²The bank may adjust the loan amount A_t by selling loans in the secondary market. The technological progress on the reduction of information asymmetries between loan buyers and loan sellers facilitate the trading of loans, and the design of contract between the loan buyers and originators can alleviate the moral hazard problem (reduced monitoring incentive) on the part of loan originators (e.g., Pennacchi, 1988; Gorton and Pennacchi, 1995).

market (i.e., $B_t < 0$) and earns the interest rate r . We can rewrite the law of motion for K_t as

$$dK_t = (X_t + K_t) \left[(r + \frac{A}{t} - A) dt + \frac{A}{t} dW_t^A \right] - X_t i_t dt - C(n(i_t); X_t) dt - dU_t + dF_t: \quad (11)$$

Given the Markov nature of the bank's problem, we suppress the time subscript of X and K going forward to simplify the notations wherever it does not cause confusion.

Payout and Equity Issuance. The bank pays out dividends, i.e., $dU_t > 0$, only if the decrease of continuation value is equal to or less than the consumption value of dividends, $V(X; K) - V(X; K - dU_t) \leq dU_t$; i.e.,

$$V_K(X; K) \leq 1: \quad (12)$$

The optimality of payout also requires the following smooth-pasting condition:

$$V_{KK}(X; K) = 0: \quad (13)$$

The bank raises equity, i.e., $dF_t > 0$, only if the increase of shareholders' value after issuance is equal to or greater than the cost,

$$V(X; K + dF_t) - V(X; K) \geq dF_t + dH_t = \alpha_0 X + (1 + \alpha_1) M_t: \quad (14)$$

where $dF_t = M_t$ is the capital raised and, as previously discussed, the issuance costs have a fixed and a proportional components, $dH_t = \alpha_0 X + \alpha_1 M_t$. The fixed cost is set to be proportional to X_t , i.e., the size of the bank, to avoid it being negligible as all balance-sheet variables grow exponentially. The optimal amount of issuance is given by the following condition:

$$V_K(X; K + M_t) = 1 + \alpha_1: \quad (15)$$

HJB Equation. Given the laws of motion (2) for X and (11) for K , in the interior region where $dU_t = 0$ and $dF_t = 0$, the bank's HJB equation is

$$\begin{aligned} V(X; K) = & \max_{f, A; R; i; g} V_X(X; K) X [-X + n(i)] + \frac{1}{2} V_{XX}(X; K) X^2 \frac{\sigma^2}{X} \\ & + V_K(X; K) (X + K) (r + A - A) + \frac{1}{2} V_{KK}(X; K) (X + K)^2 \left(\frac{A}{A} \right)^2 \\ & - V_K(X; K) [Xi + C(n(i); X)] + V_{XK}(X; K) X(X + K) \frac{A}{A} \frac{A}{X} : \end{aligned} \quad (16)$$

Lending. The first-order condition for A gives the following solution:

$$A = \frac{A + (X; K) \frac{A}{X}}{(X; K) \frac{2}{A} \left(\frac{X+K}{K} \right)} ; \quad (17)$$

where we define

$$(X; K) \equiv \frac{-V_{KK}(X; K) K}{V_K(X; K)} ; \quad (18)$$

the endogenous relative risk aversion, and

$$(X; K) \equiv \frac{V_{XK}(X; K) X}{V_K(X; K)} ; \quad (19)$$

the elasticity of marginal value of capital, $V_K(X; K)$, to deposits. Even though the bank evaluates the equityholders' payoffs with a risk-neutral objective in (4), it can be effectively risk-averse, i.e., $(X; K) > 0$, due to the equity issuance cost. When $(X; K) > 0$, deposits and capital are complementary in creating value for banks' shareholders.

While setting up $A = A/(X + K)$ as the control variable is convenient for solving the model, it is intuitive to express the solution in loan-to-capital ratio, i.e., $A/K = A/(X + K) = K$:

$$\frac{A}{K} = \frac{A + (X; K) \frac{A}{X}}{(X; K) \frac{2}{A} \frac{A}{K}} ; \quad (20)$$

This solution resembles Merton's solution of portfolio choice. In the numerator, a higher risk-adjusted excess return, A , increases lending. The bank's incentive to lend is also strength-

ened when deposits are natural hedge – the asset-side shock, $d\mathcal{W}^A$, and the liability-side (deposit) shock, $d\mathcal{W}^L$ are positively correlated ($\rho > 0$) and more deposits make capital more valuable (i.e., $(X; K) > 0$).¹³.

Deposit rate. The bank sets the deposit rate, i , to equate the marginal value of new deposits, $V_X(X; K) n^\theta(i) X$, and the marginal costs from reducing the shareholders' profits (i.e., return on equity capital) by paying interests on the existing deposits, $V_K(X; K) X$, and by paying the costs of maintaining a larger deposit franchise, $V_C(n(i); X) n^\theta(i)$:

$$V_X(X; K) n^\theta(i) X = V_K(X; K) [X + C_n(n(i); X) n^\theta(i)] : \quad (21)$$

4.2 Optimal Deposit Rate

First, we specify the deposit demand as

$$n(i) = \beta i; \quad (22)$$

where, as shown in (2), β is the semi-elasticity of deposits X_t with respect to i , which we will calibrate to the estimate from Drechsler, Savov, and Schnabl (2017) in our numeric solution. Next, we specify the deposit maintenance/adjustment cost as follows,

$$C(n(i); X) = \left(c_0 + \frac{1}{2} n(i)^2 \right) X : \quad (23)$$

The cost is increasing in the existing amount of deposits, X_t , and is increasing and convex in the flow of new deposits $n(i)$, reflecting the increasing marginal cost of expanding the depositor base.

This functional form leads to a Hayashi style optimal policy of deposit rate. In Hayashi (1982), firms make investments in productive capital, while, in our model, the bank attracts depos-

¹³While different in mechanism, this feature of our model echoes the literature on the synergy between lending and deposit-taking (see, e.g., Calomiris and Kahn, 1991; Berlin and Mester, 1999; Kashyap, Rajan, and Stein, 2002; Gatev and Strahan, 2006; Hanson, Shleifer, Stein, and Vishny, 2015)

itors by raising the deposit rate, building up its customer capital. Using (21), we obtain

$$i = \frac{\frac{V_X(X;K)}{V_K(X;K)} - \frac{1}{I}}{1} ; \quad (24)$$

Consistent with the evidence in Drechsler, Savov, and Schnabl (2017), the deposit rate is higher when the demand is more elastic, i.e., I is high. The bank also sets a higher rate to attract more deposits when the marginal adjustment cost increases slowly, i.e., β is low.

The bank sets a high deposit rate when the marginal value of deposits, $V_X(X;K)$, is high relative to the marginal value of equity capital, $V_K(X;K)$. Paying a higher deposit rate attracts more deposits but paying more interest expenses reduce earnings and equity. Section 3 presents the solution of the bank's problem without the equity issuance costs. In that case, the marginal value of equity is always equal to one and the marginal value of deposits is a constant Q . Therefore, the optimal rate is a constant:

$$i = \frac{Q - \frac{1}{I}}{1} ; \quad (25)$$

In the presence of equity issuance cost, the optimal policy of deposit rate depends on X and K .¹⁴

An interesting feature of the optimal deposit rate is that it hits the zero lower bound when

$$\frac{V_X(X;K)}{V_K(X;K)} \leq \frac{1}{I} ; \quad (26)$$

Once the deposit rate reaches zero, the bank cannot further decrease the deposit rate to reduce deposits. Later we show that this restriction makes deposits undesirable, especially when the bank is undercapitalized, and thus, is afraid that a high leverage due to large deposit liabilities amplifies the impact of negative shocks on equity, increasing the likelihood of costly equity issuance. When the deposit demand is more elastic, i.e., I is high, the bank has to pay a higher deposit rate, as shown in (24), which turns to decrease the shareholders' value. However, given the value function, it is less likely for the condition (26) to hold, because a high demand elasticity allows the bank to

¹⁴The difference between (24) and (25) is akin to the difference in a firm's optimal investment in Hayashi (1982) and Bolton, Chen, and Wang (2011). In Bolton, Chen, and Wang (2011), the cost of raising equity induces a state-dependent value of liquidity, so the ratio of marginal value of capital to that of liquidity drives the firm's investment.

control the deposit flow more effectively and thereby to avoid hitting the zero lower bound. Our numeric solution will show which force dominates given the calibrated parameter values.

4.3 Optimal Risk-Taking

Given the functional forms of payment settlement costs and deposit maintenance costs, the bank's problem is homogeneous in X and its value function $V(X; K) = v(k) X$, where

$$k = \frac{K}{X}; \quad (27)$$

Therefore, instead of working with X and K as the state variables, we will work with X and k . The capital-to-deposit ratio, k , captures the composition of long-term funding on the liability side of the bank's balance sheet. We will show that the choice variables are functions of k only.

Next, we simplify the expression of loan-to-capital ratio, a measure of the bank's risk-taking. First, note that the expression of the effective risk aversion in (18) can be simplified to

$$\rho(k) = \frac{-V_{KK}(X; K) K}{V_K(X; K)} = -\frac{v''(k) k}{v'(k)}; \quad (28)$$

And, the elasticity of marginal value of capital to deposits in is given by (19)

$$\eta(k) = \frac{V_{XK}(X; K) X}{V_K(X; K)} = -\frac{v''(k) k}{v'(k)}; \quad (29)$$

which happens to be equal to $\rho(k)$.

Using $\eta(k) = \rho(k)$, we simplify the optimal loan-to-capital ratio from (20):

$$\frac{A}{K} = \frac{A}{(k) \frac{2}{A}} + \frac{X}{A}; \quad (30)$$

The bank's risk-taking is state-dependent and only depends on k through $\rho(k)$. When the effective risk aversion is low, the bank chooses a high loan-to-capital ratio; when the effective risk aversion is high, the bank reduces its risk exposure. In our numeric solution, we show that $\rho(k)$ decreases

in k , so the loan-to-capital ratio increases when the bank has a high equity buffer relative to its deposit liabilities. The correlation between the loan return shock and the deposit flow shock, ρ , induces a hedging demand. The risk of deposit flow is essentially the bank's background risk from the perspective of portfolio management.

4.4 Solving the Value Function

The Value Function ODE. To solve the bank's value function, we simplify the HJB equation to obtain an ordinary differential equation for $v(k)$. First, given that $V(X; K) = v(k)X$, we obtain

$$\begin{aligned} V_K(X; K) &= v^\rho(k) ; V_X(X; K) = v(k) - v^\rho(k)k \\ V_{KK}(X; K) &= v^{\rho\rho}(k) \frac{1}{X} ; V_{XX}(X; K) = v^{\rho\rho}(k) \frac{k^2}{X} ; V_{XK}(X; K) = -v^{\rho\rho}(k) \frac{k}{X} \end{aligned} \quad (31)$$

Using these expressions, we can rewrite the HJB equation (16) as

$$\begin{aligned} v(k) = \max_{A, i} & [v(k) - v^\rho(k)k](-x + !i) + \frac{1}{2}v^{\rho\rho}(k)k^2 \frac{2}{X} \\ & + v^\rho(k)(1+k)(r + A_A) + \frac{1}{2}v^{\rho\rho}(k)(1+k)^2 \left(\frac{A}{X} \right)^2 \\ & - v^\rho(k) \left[i + \sigma_0 + \frac{1}{2}(\sigma !)^2 \right] - v^{\rho\rho}(k)k(1+k) \frac{A}{X} \end{aligned} \quad (32)$$

To show that (32) is an ODE for $v(k)$, we need to show that the control variables only depend on k and the level and derivatives of $v(k)$. First, by definition, $A = A(X + K)$, so we obtain the following simplified expression for A from (30):

$$A = \left(\frac{A}{K} \right) \left(\frac{K}{K + X} \right) = \left(\frac{A}{(k) \frac{2}{A}} + \frac{X}{A} \right) \left(\frac{k}{1+k} \right) \quad (33)$$

The optimal deposit rate given by (24) only depends on $V_X(X; K) = v(k) - v^\rho(k)k$ and $V_K(X; K) = v^\rho(k)$. Then we can substitute these optimal choices into the HJB equation to obtain a second-order ODE for $v(k)$ that contains only k and the level and derivatives of $v(k)$. Fully solving the model then takes two steps, first, solving the ODE to obtain $v(k)$, and second, using the solved

$v(k)$ and its derivatives to solve the bank's optimal choices.

Boundary conditions. Let \bar{k} and \underline{k} denote respectively the dividend payout and issuance boundaries, and let $m \equiv M/X$ denote the amount financing raised via issuance (scaled by X). The boundary conditions implied the optimality condition on payout (12) and (13) are

$$v'(\bar{k}) = 1; \quad (34)$$

and the smooth-pasting condition,

$$v''(\bar{k}) = 0; \quad (35)$$

The boundary conditions implied by the optimality condition on issuance (14) and (15) are

$$v(\underline{k} + m) - v(\underline{k}) = \beta_0 + (1 + \beta_1) m; \quad (36)$$

and

$$v'(\underline{k} + m) = 1 + \beta_1; \quad (37)$$

Our numerical solution of $v(k)$ features global concavity, so (34) and (37) imply that $\bar{k} > \underline{k}$. Given \underline{k} , the four boundary conditions above solve the second-order ODE for $v(k)$ (i.e., the HJB equation), the upper boundary \bar{k} , and the endogenous issuance amount m . However, we still need one condition to pin down \underline{k} . In our numerical solution, $v(k)$ is globally concave, so $\underline{k} = 0$, i.e., the bank does not pay the issuance costs unless its capital drops to zero. However, in the presence of leverage ratio requirement, \underline{k} must be positive. In our numerical solution, when k is small, $B < 0$ so the leverage ratio constraint implies that $(K + X) = K \leq L$, i.e.,

$$k \geq \underline{k} = \frac{1}{1 - \beta_L} - 1; \quad (38)$$

Table 1: PARAMETER VALUES

This table summarizes the parameter values for our baseline analysis. Whenever applicable, parameter values are annualized.

Parameters	Symbol	Value
risk-free rate	r	2%
discount rate		13%
bank excess return	λ_A	0.7%
asset return volatility	σ_A	10%
average duration of deposits	$1 = \lambda_X$	20 years
deposit flow volatility	σ_X	20%
correlation between deposit and asset shocks		0.6
deposit demand semi-elasticity	β	5.3
deposit maintenance cost (linear component)	θ_0	-0.03
deposit maintenance cost (quadratic component)	θ_1	0.5
equity issue fixed cost	θ_0	1.0%
equity issue propositional cost	θ_1	5.0%
capital regulation parameter		14.3

5 Quantitative Analysis

5.1 Parameter Choices

One unit of time is set to one year. We choose r equal to 2% in line with the historic average of fed fund rate since 1990s. The spread between shareholders' required return and the risk-free rate, $\lambda - r$, has several components. First, as previously discussed, it includes a Poisson-arriving death rate. We set this component to 7% following Gertler, Kiyotaki, and Prestipino (2019). Second, the shareholders require a risk premium, which we set to 4%, consistent with a bank beta of 0.7 (Fahlenbrach, Prilmeier, and Stulz, 2012) and an average of equity premium around 6%. Therefore, λ is equal to 13%, which is the sum of risk-free rate (2%), the exit rate (7%), and the shareholders' required compensation for systematic risk (4%). We set λ_A to 0.7% in line with the estimate of Begenau (2019). We set asset-value volatility, σ_A , to 10% following Sundaresan and Wang (2014) who in turn refer to the calculation of Moody's KMV Investor Service.

On the deposit dynamics, we set σ_x to 5% and $\sigma_{\dot{x}}$ to 20% so the mean and volatility of deposit growth rate are in line with the calibration of Bianchi and Bigio (2014). We set β , the semi-elasticity of deposits with respect to the deposit rate, to 5:3, which is the estimate from Drechsler, Savov, and Schnabl (2017). We set δ , the cost of maintaining existing deposits, to -0.03 so the model generates an average deposit-to-capital ratio in line with data (FRED). We adjust γ to 0.5 so the model generates an average deposit rate that matches data (Driscoll and Judson, 2013). The correlation between asset-side shock and liability-side (deposit) shock is set to 0.6 so that the model generates an average loan-to-deposit ratio that matches the data (FRED). We set the proportional issuance cost is 5% (Boyson, Fahlenbrach, and Stulz, 2016) and the fixed cost 1%. The regulatory parameter was discussed in Section 2.

5.2 Franchise Value

In perfect capital markets, the bank shareholders' value, V_t , is equal to book equity, K_t . In the presence of equity issuance costs, the bank has to maintain a positive level of profits whose present value justifies paying the cost to raise equity. The issuance costs thus create a wedge between V_t and K_t , which we call the franchise value. In Panel A of Figure 1, we plot the wedge (scaled by the deposit stock X_t) against k , the ratio of bank capital to deposits. As capital accumulates relative to deposits, the franchise value increases. The comovement between franchise value and equity capital is consistent with the evidence from Boyson, Fahlenbrach, and Stulz (2016).

The bank pays the issuance costs at the lower bound of k , \underline{k} , when capital is significantly depleted relative to deposits. The further away it is from the issuance boundary, the lower the likelihood of hitting the boundary and paying the issuance costs. Therefore, the franchise value increase in k . The curve ends on the right side at the dividend payout boundary \bar{k} . Because the likelihood of paying the issuance cost is low near \bar{k} , the franchise value is relatively insensitive to the variation of k . Our results have several implications on the empirical analysis of bank valuation (e.g., Minton, Stulz, and Taboada, 2019). First, instead of book equity as the nominator of valuation metric, deposit stock emerges as the natural denominator. Second, scaled by deposits, the shareholders' value increases in the capital-to-deposit ratio, reaching its highest level when

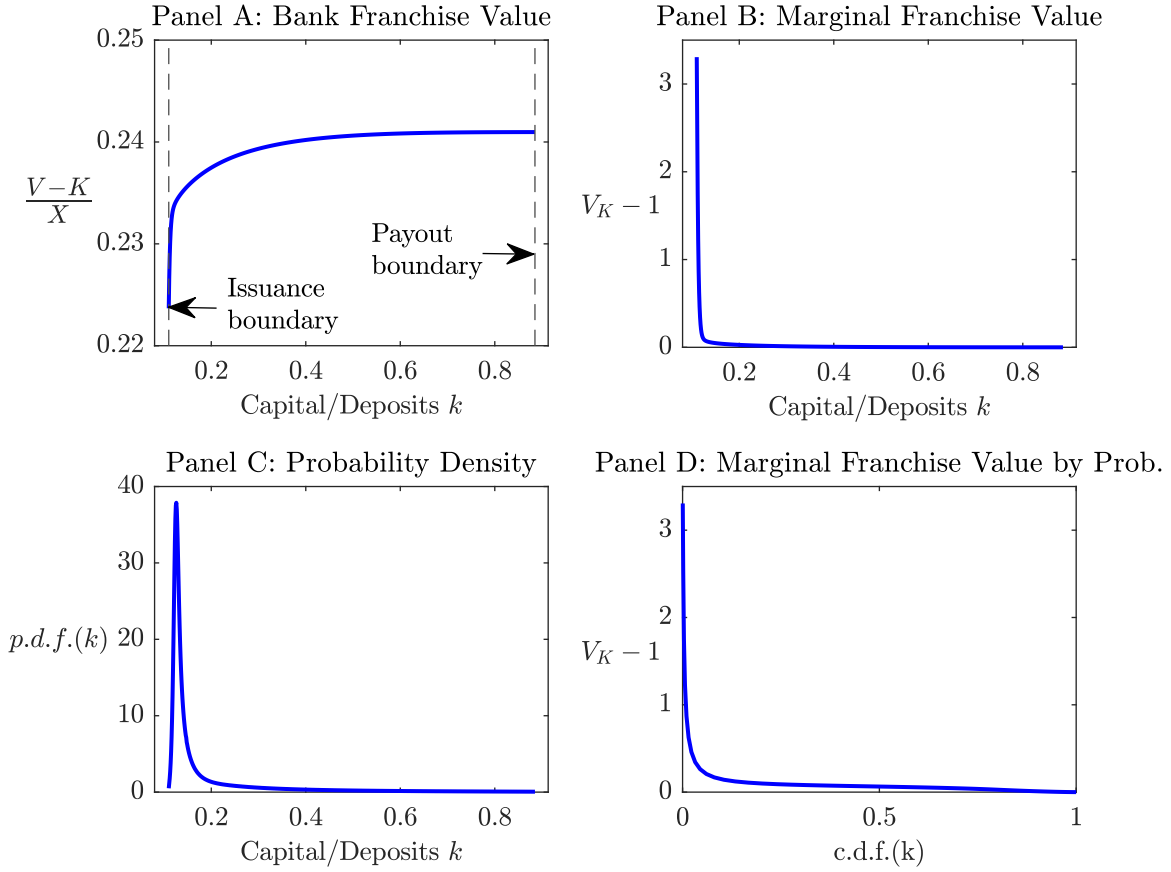


Figure 1: The Shareholders' Value and Book Value of Bank Capital

the bank pays out dividends and falling to its lowest level when the bank raises equity. This is consistent with the evidence that bank value is procyclical while equity issuance is countercyclical (Adrian, Boyarchenko, and Shin, 2015; Baron, 2020).

Panel B of Figure 1 plots the marginal franchise value of bank capital, $V_K - 1$. Without financial frictions, this variable should always be equal to zero as $V_t = K_t$. However, near the issuance boundary, the marginal value of equity capital shoots up dramatically. At \underline{k} , a value of $V_K - 1$ larger than three means that one dollar of equity is worth four dollars because the imminence of costly equity issuance. Note that even though the proportional cost of issuance is only 5%, due to the fixed cost (0.01), the value of one dollar equity can be more than 300% higher than one.

Panel C of Figure 1 plots the stationary probability density of the state variable k . It shows that in the long run, how much time the bank spends in various regions of k . The probability mass is highly concentrated in the area where k is still sufficiently large and the marginal value of equity is low. In fact, the density function peaks at the k where the marginal value of equity is only 1.0851, i.e., $V_k - 1$ equal to 0.0851. Therefore, even though for the majority of time, the bank does not seem to be financially constrained, the shadow value of equity shoots up dramatically when equity is significantly depleted, showing a sharp contrast between normal time and crisis period. Panel C of Figure 1 is likely to have underestimated the shadow value of internal capital for banks because, in crisis, the equity issuance costs are likely to increase (Bolton, Chen, and Wang, 2013) but in our model, we only consider the constant issuance costs.

In Panel D of Figure 1, we plot the marginal franchise value of bank capital against the cumulative distribution function of k . In the graph, the horizontal span of the curve represents the amount of time the bank spends in this region on the long run. For example, the bank spends half of the time in the region to the right of 0.5 with a marginal franchise value of capital below 0.0634, i.e., one dollar of equity worth below 1.0634 dollars. However, on the left side (from 0 and 0.01), the bank spends 1% of time with the one dollar of equity worth more than 1.8702 dollars, i.e., a marginal franchise value of 0.8702 or higher. Crisis is rare event but its impact is significant.

In Figure 2, we analyze the bank's risk-taking. Panel A plots the ratio of loan value to capital. It cannot exceed the regulatory upper bound from the capital requirement. Risk-taking is strongly procyclical. As capital accumulates relative to deposits, i.e., k , increases, the bank levers up quickly through deposits and the issuance of short-term bonds and invest in risky loans. If capital is depleted relative to deposits, the bank deleverages. This is consistent with the findings of Ben-David, Palvia, and Stulz (2020) that distressed banks deleverage and decrease observable measures of riskiness, in contrast to the prediction of moral hazard or gambling for resurrection.

An intuitive measure of the risk-taking incentive is $\gamma(k)$, the relative risk aversion coefficient of the bank's value function that is defined in (18). As shown in Panel B of Figure 2, $\gamma(k)$ shoots up dramatically as the bank becomes undercapitalized. In Panel C and D, we plot the loan-to-capital ratio and $\gamma(k)$ against the c.d.f. of k shows how much time the bank spends in different

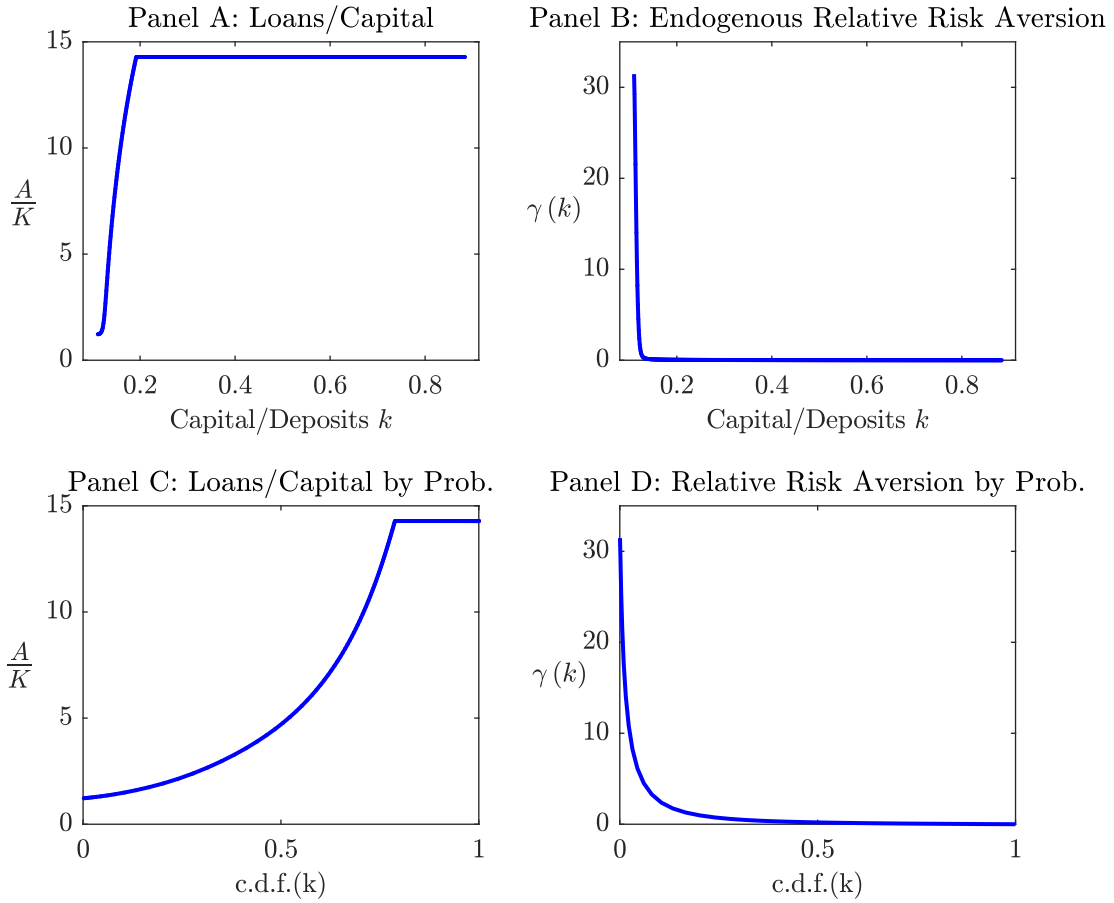


Figure 2: Risk-Taking

regions. In Panel D, more than 50% of the time, the bank's relative risk aversion is below 0.2 (in the region right to 0.5), but in 1% of the time (the region from 0 to 0.01), the bank's relative risk aversion is beyond 17.6.

Panel A of Figure 3 plots the marginal value of deposits, i.e., $V_X(X; K) = v(k) - v'(k)k$, which we call *deposit Q*. When the bank has ample capital relative to deposits, i.e., k is large, the deposit Q is positive. According to Panel C where the deposit Q is plotted against the c.d.f. of k , the deposit Q is above 0.19 more than 97% of the time (i.e., to the right of 0.1 on the X-axis). Deposit financing is cheaper than short-term borrowing at the rate r . In Panel B of Figure 3, we compare the risk-free rate and the deposit rate. The spread reflects the bank's deposit market

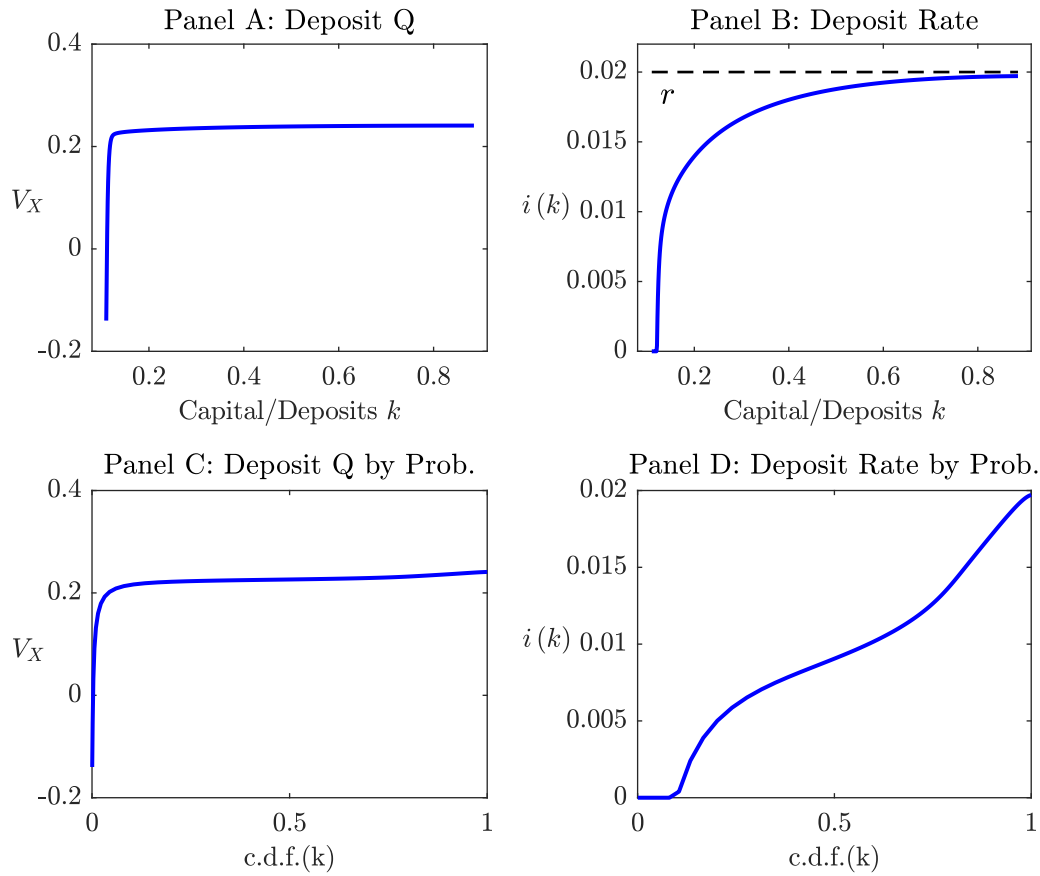


Figure 3: The Value of Deposits

power (Drechsler, Savov, and Schnabl, 2017) and depositors valuing deposits for the convenience of making payments. When the bank has sufficient capital to buffer risk, deposits create value by allowing the bank finance risky lending with relative cheap sources of funds. The deposit stock serves as a form of productive capital for the bank. When k is sufficiently large, the bank is willing to set a high deposit rate to attract depositors. The comovement of loan growth (Panel A of Figure 2) and deposit rate increase (Panel B of Figure 3) is consistent with the finding of Ben-David et al. (2017). As shown in Panel D of Figure 3, the bank spends relative equal amount of time across different values of deposit rate, except that at the zero lower bound, there is a point mass.

A very interesting finding is that the deposit Q can turn negative when bank capital is low

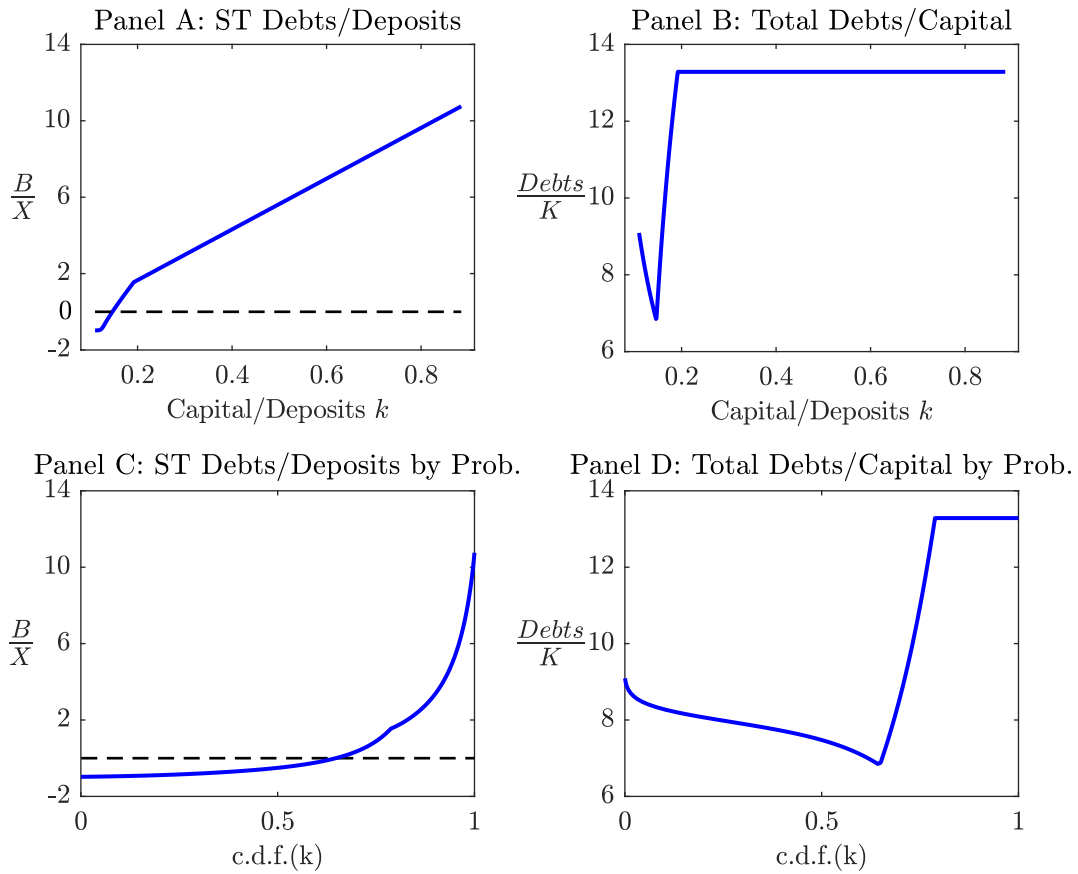


Figure 4: Debt and Leverage

relative to the deposit stock. The reason is that when k is near the equity issuance boundary, deposits destroy value for the bank's shareholders by forcing the bank to sustain a high level of leverage that amplifies the impact of shocks on bank capital and makes it more likely to incur costly equity issuance. The bank may want to delever, turning away deposits by lowering the deposit rate. However, as shown by Panel B of Figure 3, doing has a limit, that is the zero lower bound of deposit rate. Setting a deposit rate below zero causes depositors to withdraw deposits en masse and hoard dollar bills (which has a zero return). While we do not explicitly model the consequence of a run, the value destroyed through liquidation of loans and fire sale is likely to make the zero lower bound a binding constraint for the bank. Therefore, to reduce leverage, the

best that the bank can do is to set deposit rate to zero.

Deposits are very different from short-term debts. For short-term debts, the bank can always choose to stop borrowing at maturity, and therefore, does not face the problem of unwanted debts. However, deposit contracts do not have maturity. Deposits leave the bank only when depositors withdraw dollar bills or make payments to those who do not hold accounts at the bank. As long as depositors are willing to hold deposits, the bank cannot turn away the existing depositors. After hitting the zero lower bound, the bank loses control of its leverage.

Figure 4 analyzes the the bank's debt structure. Panel A plots the ratio of short-term bond to deposits, and Panel C reports the ratio over the c.d.f. of the state variable k . When capital is abundant relative to deposits, the bank raises funds from short-term debts for risky lending, while when capital is relatively scarce, the bank switches its short-term debt position, holding risk-free debts to reduce the overall riskiness of its asset portfolio. When k is small and the deposit rate reaches the zero lower bound, the bank loses control of its leverage, and therefore, has to work on the asset-side of its balance sheet, tuning down its risk exposure by holding risk-free assets, in order to reduce the likelihood of costly equity issuance. As shown in Panel B of Figure 4, once the bank has stopped borrowing short-term debts and deposits become the only type of debts, a further decline of $k = K=X$ induces a lock-step increase of leverage $X=K$.

6 Policy Implications and Future Research

6.1 Outside Money and Financial Stability

Depositors hold deposits as means of payment. The payment functionality of deposits has two impacts on the bank. First, the bank faces uncertainty (driven by payment flows) in the stock of deposit liabilities. Second, as shown in Panel B of Figure 3, depositors enjoy the payment convenience, and thus, are willing accept a deposit rate that is below the prevailing interest rate r , so the bank can finance lending cheaply. Overall, deposits add value *if* the bank is well capitalized. When capital is significantly depleted due to bad shocks to the loan portfolio, deposits become burden and the marginal value of deposits turn negative as shown in Panel A of Figure 3.

An undercapitalized bank loses its control over leverage once it hits the zero lower bound on the deposit rate. The variation of deposit stock on the liability side of its balance sheet is completely at the mercy of depositors. The bank can be liberated if depositors decide to withdraw faster, which, through the lens of the model, translates into a higher rate of λ . When the deposit Q , $V_X(X; K)$ is negative, deposit outflow actually adds value to the bank, i.e., $V_X(X; K) \lambda dt > 0$, by reducing the leverage and the risk of costly equity issuance.

One way to achieve faster deposit withdrawal rate is to provide depositors alternative monetary assets to hold. The government may increase its supply of short-term government bonds when the banking sector is undercapitalized, which was exactly what we observed in the aftermath of the global financial crisis. Government securities have long been recognized as money-like especially when investors hold them through the money-market mutual funds.¹⁵ As long as government securities are not perfect substitutes of deposits in terms of the payment convenience, depositors will not withdraw en masse to pursue the positive yield on government securities but only rebalance their portfolio by reducing the weight on deposits. Therefore, an increase of supply of government securities can actually stabilize banks by reducing their leverage when banks are undercapitalized.

This implication of our model stands in contrast with Li (2019) who shows that the money-like securities issued by the government crowd out banks' profits from issuing money-like securities, and thereby, delay the accumulation of bank capital, prolonging financial crises. Our model differs from Li (2019) in two aspects. First, we differentiate the short-term debts and deposits that feature a lower bound on the interest rate and stochastic maturity, while Li (2019) studies banks' standard short-term debt with a money premium (or convenience yield) attached to it. Second, Li (2019) endogenizes the risk-free rate while we analyze a partial equilibrium with r fixed.

Our result that government securities, by crowding out banks' money-like liabilities, stabilize the banks echoes Greenwood, Hanson, and Stein (2015) and Krishnamurthy and Vissing-Jørgensen (2015). However, we obtain our result in a fully dynamic setting and our result is derived from the special contractual features of deposits: (1) deposits have stochastic maturity that banks cannot

¹⁵The monetary service of government liabilities is an old theme (e.g., Patinkin (1965); Friedman (1969)). Recent contributions include Bansal and Coleman (1996), Bansal, Coleman, and Lundblad (2011), Krishnamurthy and Vissing-Jørgensen (2012), Greenwood, Hanson, and Stein (2015), Bolton and Huang (2016), and Nagel (2016).

completely control; (2) deposit rate has a lower bound.

6.2 Banks' Demand of Safe Assets

Banks lose control of their leverage once they hit the deposit zero lower bound, so, in order to reduce the risk exposure of bank capital, banks rebalance their asset portfolio towards risk-free assets (as shown in Panel A of Figure 4). Such portfolio rebalancing of undercapitalized banks creates a demand for safe assets in financial crises. The government is in a unique position to supply such assets. In a general equilibrium setting, the interest rate r is endogenous, so banks' demand for safe assets is likely to push downward the interest rate, reducing the government's financing cost. The government can thus issue more debts, meeting the banks' demand, and then use the proceeds from debt issuance to stimulate the economy. During the height of the global financial crisis, the supply of U.S. Treasury bills tripled, and banks significantly increased their holdings of Treasury securities, which were then sold to the Federal Reserve (Fed) in exchange for interest-paying reserves as the Fed conducted quantitative easing by purchasing Treasury securities.

Undercapitalized banks' portfolio rebalancing towards safe assets is necessary because of the special features of deposits. Effectively, banks are performing a liquidity transformation for the non-financial sector. They hold risk-free assets that do not directly serve as means of payment, while have on the liability side of their balance sheets the deposits that the non-financial sector use to settle transactions. The unique position of banks in the payment system is the root of banks' demand for safe assets in crises. As discussed in the previous subsection, if depositors have close substitutes to hold in stead of deposits as means of payment, banks can off-load deposit liabilities, and thereby, having a weaker need for safe assets. In fact, the modern reforms of payment system facilitate such transition. Instead of having banks holding safe assets and issuing deposits, money market funds allow the non-financial sector to hold safe assets directly and then use money-market fund shares as close substitutes of deposits to make payments.

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A Solving the Model without Equity Issuance Costs

By inspecting the HJB equation (16), we know that when the value function is linear in K , the bank maximizes A (and borrow short-term debts) as long as $A > 0$. Therefore, A is the bank's total assets and the capital requirement and SLR restriction coincide (as we assume $\kappa = \ell$) and bind, i.e., $A=K = \kappa$ (or $A(1 + \frac{1}{\kappa}) = \kappa$). The optimal deposit rate is given by (24):

$$i = \frac{Q - \frac{1}{\ell}}{1} ; \quad (39)$$

Next we solve Q using the HJB equation (16) under the conjecture of value function $(k + Q)X$:

$$k + Q = Q(-x + \ell i) + r + rk + \kappa A - \left[i + \frac{1}{2} (\ell i)^2 \right] ;$$

For this equation to hold, we need the following quadratic equation to hold

$$\frac{\ell}{1} \left(1 - \frac{\ell}{2}\right) Q^2 - \left(\frac{2}{1} + x + \right) Q + r - \frac{1}{\ell} + \left(\frac{1}{\ell} + \frac{1}{2}\right) \frac{1}{1} = 0 ; \quad (40)$$

which solves Q , and the coefficient on k is equal to zero, i.e.,

$$= r + \kappa A ; \quad (41)$$

Equation (41) requires that the bank is indifferent between paying out dividend and retaining equity. If $> r + \kappa$, the bank prefers paying out dividends because the expected return on equity capital is below the shareholders' required rate of return. If $< r + \kappa$, the bank never pays dividend and prefers to raise an infinite amount of equity because the expected return on equity is greater than the shareholders' required return.

Under the condition,

$$\left(\frac{2}{1} + x + \right)^2 \geq \frac{4\ell}{1} \left(1 - \frac{\ell}{2}\right) \left[r - \frac{1}{\ell} + \left(\frac{1}{\ell} + \frac{1}{2}\right) \frac{1}{1}\right] ; \quad (42)$$

the roots of Equation (40) exist and are given by

$$Q = \frac{\left(\frac{2}{1} + x + \right) \pm \sqrt{\left(\frac{2}{1} + x + \right)^2 - \frac{4\ell}{1} \left(1 - \frac{\ell}{2}\right) \left[r - \frac{1}{\ell} + \left(\frac{1}{\ell} + \frac{1}{2}\right) \frac{1}{1}\right]}}{\frac{2\ell}{1} \left(1 - \frac{\ell}{2}\right)} ; \quad (43)$$

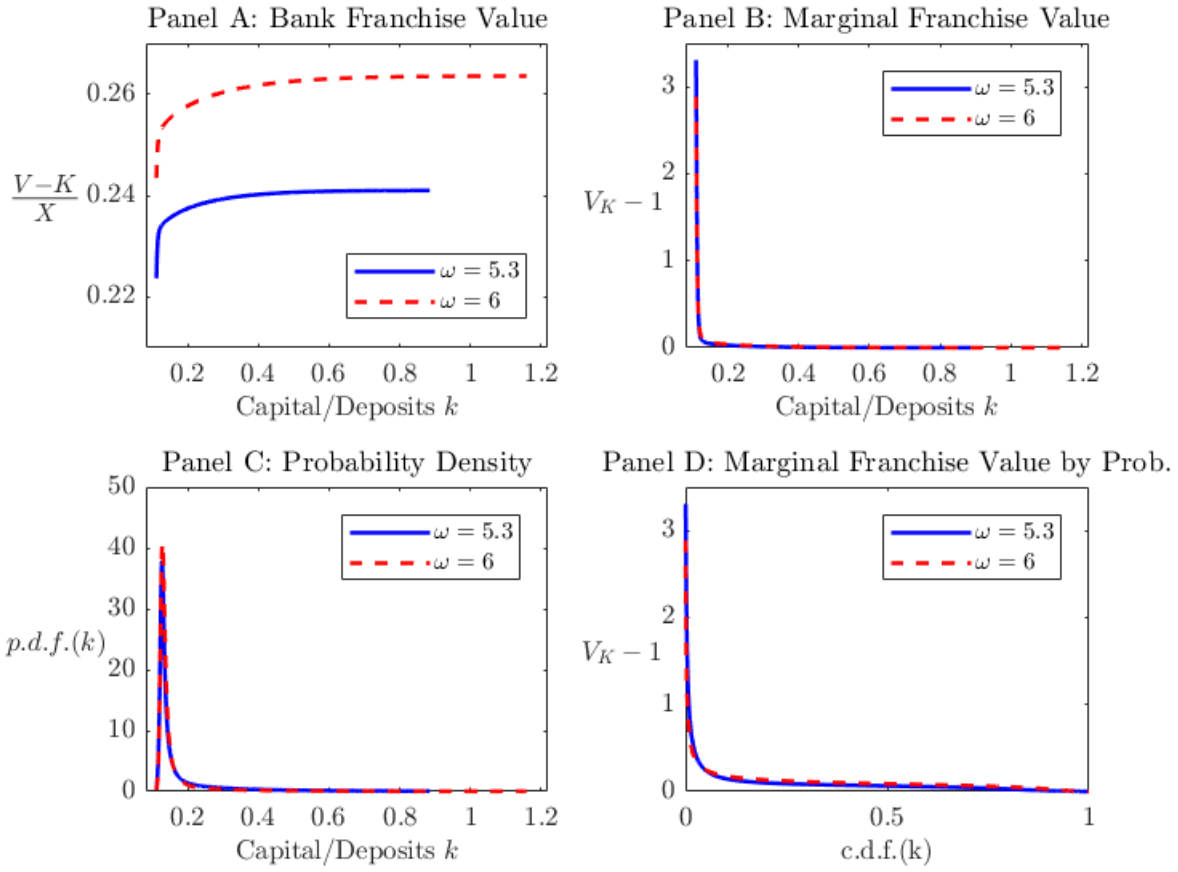


Figure 5: Deposit Demand Elasticity and the Value of Bank Capital

B Deposit Demand Elasticity, Cost of Deposits, and Risk-Taking

There is an unsettled debate on how competition affects banks' lending on both the theoretical and empirical fronts (Keeley, 1990; Petersen and Rajan, 1995; Jayaratne and Strahan, 1996; Allen and Gale, 2004a; Boyd and De Nicoló, 2005; Bertrand, Schoar, and Thesmar, 2007; Erel, 2011; Scharfstein and Sunderam, 2016; Drechsler, Savov, and Schnabl, 2017; Liebersohn, 2017). Our model shows a particular force that suggests more competition in the deposit market results in more caution in risk-taking, especially through the delaying of payout to shareholders.

In our baseline solution, we set ω to 5.3, an estimate from Drechsler, Savov, and Schnabl (2017). In Figure 5, we compare the franchise value and the marginal value of bank capital of the baseline case and the solution with a higher deposit demand elasticity, $\omega = 6$. Under a more elastic demand for deposits, the bank can adjust the deposit flow more easily by setting the deposit rate. As shown in Panel A of Figure 5, a more elastic demand for deposits increases the bank's

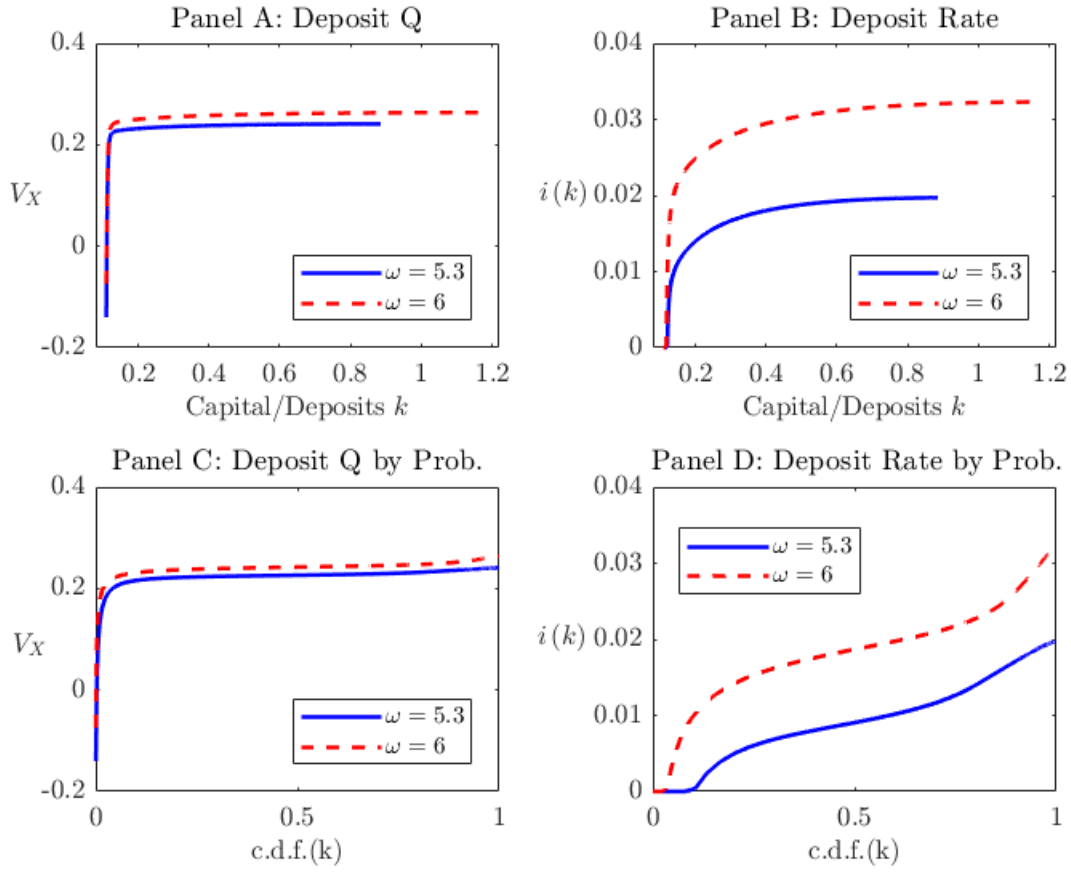


Figure 6: Deposit Demand Elasticity and the Value of Deposits

value because a prominent problem of deposit liabilities is that the maturities are largely out of the bank’s control, especially so when the deposit rate has already hit the zero lower bound.

Panel B and D of Figure 5 shows that the marginal value of bank capital is quite insensitive to the change of ω . Therefore, the increase of bank value in Panel A can be largely attributed to a higher value of deposits as the bank’s value function depends on only two state variables, capital K and deposit X . In Panel C of Figure 5, we show that the distribution of state variable k is extended to the right. Accordingly, in Panel A and B, the curves end at higher values of k .

The bank pays out dividends at a higher value of capital-to-deposit ratio when the deposit demand is more elastic. The bank is more eager to preserve capital because deposit is now more valuable. In Panel A of Figure 6, the marginal value of deposits is higher when the demand elasticity is higher and the deposit flow is more sensitive to the deposit rate set by the bank. To take advantage of the more flexible and valuable deposits, the bank preserves capital and delays

payout in order to stay away from the left (low k) region where the zero lower bound on deposit rate binds and the marginal value of deposit turns negative.

Consistent with the findings of Drechsler, Savov, and Schnabl (2017), a more elastic demand for deposits leads to higher deposit rate in Panel B and D of Figure 6 – when depositors are more price sensitive, the bank needs to set higher rates to attract depositors. This certainly implies a higher financing cost for banks, but, as shown in Panel A of Figure 6, the value of deposits actually increases because now the bank can better control the flow of deposits.

Under a higher elasticity of deposit demand, the bank is willing to pay a deposit rate that is above the risk-free rate (2% in our numeric solution). This seems puzzling because, if the bank can borrow cheaper in the short-term debt markets, why resorts to more expensive deposit financing? The bank pays higher deposit rates when it can afford to do so, i.e., when its capital is high relative to the deposit liability, so by building up a larger depositor base, the bank can enjoy a lower cost of financing when it is undercapitalized, i.e., when k is low. According Panel D of Figure 6, the deposit rate is still below the risk-free rate more than 50% of the time. Overall, the cost of deposits is higher when the demand elasticity is higher.

Figure 7 compares the bank's risk-taking behavior in the baseline case and the case with higher deposit demand elasticity. We see that in Panel A of Figure 7, given k , a higher cost of deposits does not significantly discourage the bank from lending, because this negative impact is offset by the positive impact of the bank having more adjustable deposit liabilities. Panel B of Figure 7 shows that given k , the bank's endogenous risk aversion is largely insensitive to the deposit demand elasticity. Panel C of Figure 7 shows that because the distribution of k changes, the bank engages in less risk-taking over the long run, consistent with the finding in Liebersohn (2017), though conditional on k , the bank's risk-taking is not significantly affected by the deposit demand elasticity as shown in Panel A.

One interesting finding is that due to the shift of probability mass towards higher values of k (and the bank's delay of paying dividends), the risk-taking has been shifted towards regions where banks are better capitalized (i.e., higher value of k). A higher demand elasticity is often associated with more intense competition for deposits among banks, so our result suggests that competition can stabilize banks by discouraging banks from payout to shareholders and taking less risks. This result is achieved without bank default. It complements the result of Keeley (1990) that competition erodes bank charter values, which in turn caused banks to increase default risk through increases in asset risk and reductions in capital.

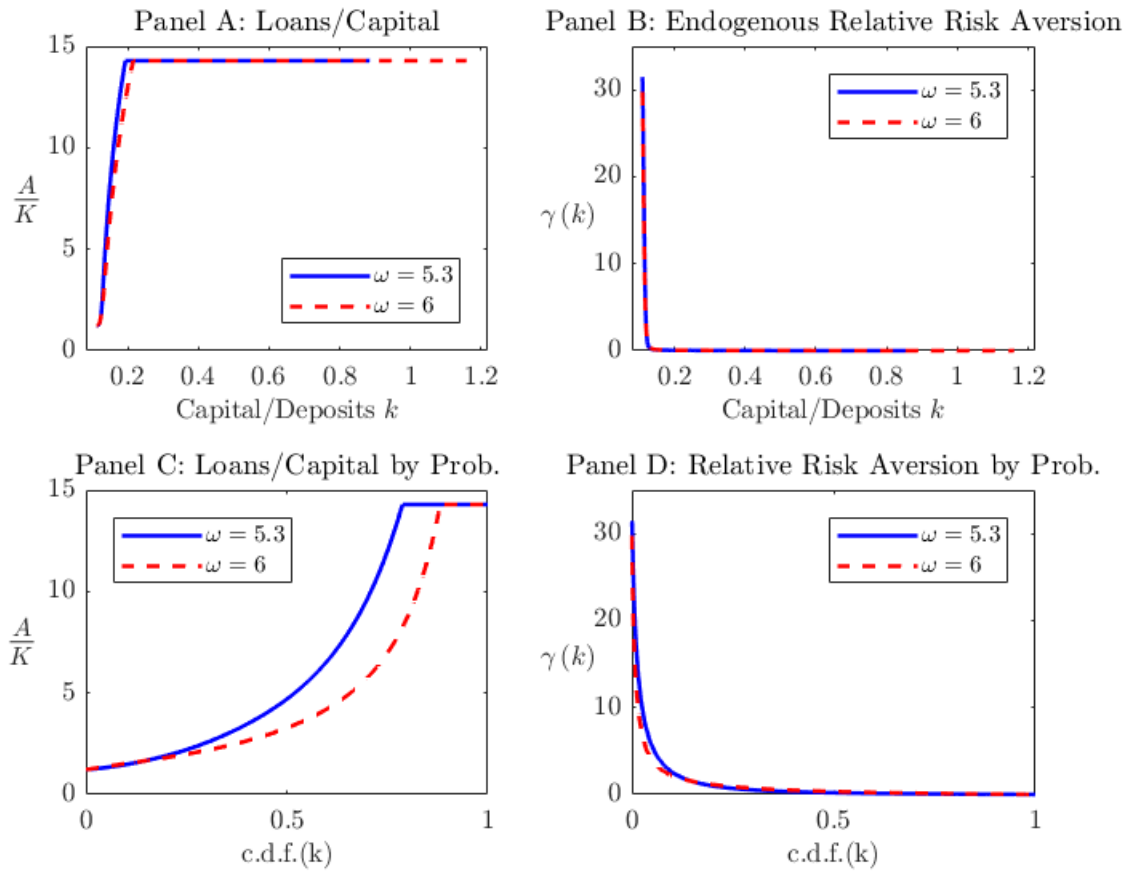


Figure 7: Deposit Demand Elasticity and Risk-Taking